

Autonomous Learning of Representations

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Abstract Besides the core learning algorithm itself, one major question in machine learning is how to best encode given training data such that the learning technology can efficiently learn based thereon and generalize to novel data. While classical approaches often rely on a hand coded data representation, the topic of autonomous representation or feature learning plays a major role in modern learning architectures. The goal of this contribution is to give an overview about different principles of autonomous feature learning, and to exemplify two principles based on two recent examples: autonomous metric learning for sequences, and autonomous learning of a deep representation for spoken language, respectively.

Keywords Representation learning · Metric learning · Deep representation · Spoken language

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1 Introduction

The ability of animate beings to autonomously learn complex models and nontrivial behaviour based on examples only has fascinated researchers right from the beginnings of machine learning and artificial intelligence. One of the striking observations which contributed to the success of early learning models such as the perceptron consisted in the fact that simple, biologically plausible principles such as Hebbian learning enable systems to provably infer a correct model from given data only. The question how neural networks internally represent these data has been a central issue: the perceptron represents information in a distributed way by encoding relevant aspects in the weights, rather than an explicit symbolic modelling. This enables a high error tolerance, taking into account multiple aspects of the data. However, the fact that the mere perceptron has very limited representation capabilities, it can represent linearly separable data only, has severely contributed to its abandoning around 1970. Back-propagation, by providing an efficient mechanism to learn a suitable distributed representation of data in one or more hidden layers, caused a neural renaissance around 1986 [57]. Multilayer networks enable a very rich internal representation, but sometimes at the costs of difficult optimisation problems for neural network training.

Interestingly, this training complexity, among other problems, accounted for the fact that the last decades have been dominated by powerful models such as the support vector machine (SVM) which is, essentially, a generalized linear map: the perceptron is enhanced by a kernel, i.e. an implicit fixed nonlinear preprocessing [12]. This avoids cumbersome training with local optima and numerical problems, since it enables a formalization of model optimization in terms of convex

quadratic programming. This approach is very successful because universal kernels exist for standard vectorial data [48, 21]; still, the choice of a suitable kernel and its parametrization for a given task can be tricky – even more so, if data are complex such as non-vectorial or symbolic data [37]. The idea of a kernel representation can be put into a line with the recent success of extreme learning or reservoir computing [16, 29, 36]. In their original form, these approaches, albeit yielding remarkable results, rely on a priorly fixed, albeit usually rich choice of a suitable data representation.

A kernel representation or nonlinear preprocessing enables highly nonlinear models as compared to the simple perceptron – still such representation has to be designed by humans, who often rely on rich universal representations such as Gaussian kernels or even random mapping rather than representations tailored for the problem at hand. Domain specific invariances such as e.g. different lightning conditions for image recognition tasks or auxiliary semantic information are usually not taken into account in this universal representation.

Since about 2006, deep neural networks with multiple stacked hidden layers started another renaissance of highly nonlinear data representation tailored for a specific domain under the umbrella term ‘deep learning’ [27, 6]. Essentially, deep learning refers to stacked nonlinear models such as neural networks or probabilistic counterparts which are characterized by a high degree of nonlinearity due to the hierarchical composition of a large number of nonlinear elements, and all elements are adaptive. It has been known since a while that such stacked systems have beneficial mathematical properties as concerns their representation ability [9, 24], however, efficient training of deep networks has long constituted a problem [7]. Novel training paradigms such as efficient unsupervised pre-training of architectures with restricted Boltzmann machines as well as a high degree of architectural regularization have recently turned such networks into efficient models. Interestingly, these models often automatically arrive at powerful internal representations of information within hidden layers, where relevant characteristics such as invariance against certain changes can be inferred based on the given data only [6, 38].

Still, the autonomous inference of a rich data representation which facilitates the design of learning systems constitutes one of the central questions in machine learning. In this contribution, we will give an overview about a number of different approaches for autonomous feature learning in the context of supervised machine learning tasks (as opposed to reinforcement learning, which is addressed in the contribution from W. Böhmer et al. in this volume). Afterwards, we will address two

specific approaches which accompany two relevant application scenarios: (1) How to autonomously adjust the metric in distance based approaches if non-vectorial data, in this case sequences, are present? An approach which extends metric learning to this setting will be presented. (2) How to infer a deep hierarchical model to represent spoken language in the case that the basic constituents such as words and phonemes are not known? We show how a Bayesian formalisation of the hierarchical concept enables the unsupervised inference of entities such as words from raw data.

2 Representation learning

There exists a variety of different principles based on which a suitable feature representation can be extracted from given data. The article [6] provides a recent review of different principles of representation learning; it summarizes diverse technologies such as the following:

(1) Deep learning has its counterparts in biological systems [34, 6, 27, 37]; deep learning essentially processes signals by means of stacked, highly regular, nonlinear transformations, which are trained to optimally represent given data sets. It turns out that the architectural constraints often enable the autonomous learning of invariances such as rotation or translation invariance and robustness to partial occlusion and lightning conditions for image recognition. Deep learning requires a sufficient number of training data, and training can be quite time consuming due to the underlying complex architectures.

(2) Sparse coding aims at efficient, meaningful representations of high dimensional signals relying on the natural bias of sparsity [28, 14, 1]; this principle makes use of the fact that many real valued signals can be represented as linear combination of few basic motifs, such as sound which can be decomposed into a sparse combination of oscillations. Sparse coding provides means to find a sparse decomposition of given signals, if existing, and to learn suitable dictionaries from observed data. Naturally, the technique is restricted to settings where such sparse approximations exist.

(3) Nonlinear dimensionality reduction formalizes the aim to represent high dimensional signals efficiently in low dimensions relying on different invariances, such as metric preservation, preservation of the probability distribution, etc. [52, 18]; dimensionality reduction plays a role as soon as data are visualized, since this requires an embedding of data in two or three dimensions. The challenge is to unravel characteristics from the data, i.e. to find a low-dimensional representation which is still meaningful. Since this problem is ill-posed unless data are intrinsically low-dimensional itself, one

of the challenges of dimensionality reduction is to find suitable regularizations for the projection; at present, no clear guidelines which dimensionality reduction technique is suitable for which data set and task exist.

(4) Highly regularized signal extraction technologies such as slow feature analysis (SFA) for the autonomous extraction of meaningful semantic entities from temporal data [58], or independent component analysis (ICA) for the extraction of independent semantically meaningful sources from mixed data [30]; both techniques put a suitable prior to the data to solve an otherwise ill-posed problem. These priors seem particularly suitable for some type of real-world data, such as the analysis of brain signals.

Besides their different objectives and application scenarios, these principles can be stratified according to different fundamental criteria, such as the following:

- Are the techniques supervised, taking into account label information for a classification task or similar, or unsupervised? Unsupervised techniques have the benefit that their results are often more general, i.e. they generate codes which can be transferred across tasks within the same domain. One interesting example for this principle are generative models such as hierarchical restricted Boltzmann machines, which can be used as excellent dimensionality reduction techniques e.g. for the visual domain [6, 27]. On the contrary, supervised approaches guarantee that the information which is used to represent the data is relevant for the task, suppressing irrelevant aspects and noise. This is particularly relevant if only few data points are available since the problem would be ill-defined without shaping it according to such auxiliary knowledge [19].
- Are the techniques linear or nonlinear; the latter can further be differentiated according to the degree of nonlinearity, ranging from generalized linear models such as kernel mappings up to deep or hierarchical models. Linear techniques have the benefit of a better efficiency, interpretability, and generalization ability; deep models, on the contrary, can easily represent topologically complex manifolds such as arise due to complex invariances in the data, for example. Interestingly, stacking networks of similar shape and parameterization leads to topological objects which resemble a fractal nature and self-similarity, a principle which is well known in the context of recurrent networks [51].
- Which type of data can the techniques deal with? Which type of representation is extracted? So far, most methods deal with vectorial signals or time series for both, input data and learned representation. Only few approaches address a richer representation

or more complex data structures such as discrete sequences or graph structures [37].

- What is the degree of autonomy for representation learning? How much training data, user interaction, and prior knowledge in terms of a Bayesian prior or the specification of an exact objective are required? Some popular representation learning techniques are fully unsupervised e.g. aiming for the most likely data representation in a probabilistic treatment such as present for deep belief networks; these methods usually require lots of given data to extract meaningful regularities. Alternatively, some approaches are fully supervised and coupled to a concrete learning task, such as feature selection for classification. Methods which display a certain degree of autonomy, which require neither big data sets nor supervised objectives, often rely on ingenious mathematical realizations of what can be seen as natural priors, such as e.g. the slowness principle in slow feature analysis, sparsity in data representation, or independence of signals in independent component analysis [58, 30, 28, 14, 1]. These priors are hand designed, and hardly any techniques exist to autonomously infer natural priors from an interaction with the environment.

3 Metric learning for sequential data

Metric learning essentially deals with the question of how to choose a metric in popular distance-based machine learning technologies such as k-nearest neighbor classifiers in an optimum way. Since an adaptation of the metric used for pairwise data comparison directly corresponds to a transformation of the data space, metric learning can be seen as one instance of representation learning. Since about 2000, metric learning rapidly advanced along different lines of research and, currently, can be considered a matured field of research for the vectorial case as summarized e.g. in the overview articles [35, 5]. Two of the earliest approaches introduce metric learning in prototype based methods: an enrichment of the unsupervised self-organizing map by a metric adjusted according to auxiliary information [32], and an enhancement of learning vector quantization to a general quadratic form which is autonomously adapted according to the classification task at hand [23]. While the former relies on the local Fisher metric and hence displays a rich capacity but also very high computational complexity, the latter restricts to a simple parameterized quadratic form. Interestingly, it can easily be generalized to local metrics, i.e. a globally nonlinear forms, and it can be accompanied by strong learning theoretical guarantees [43].

Due to its computational simplicity, quite a few techniques of how to adapt quadratic forms have been proposed in the literature afterwards; a few popular ones include the following: The approaches [59, 45] rely on side information for clustering which specifies sets of data assigned to the same cluster. Then efficient adaptation mechanisms which realise these constraints by an adjustment of a quadratic form can be derived. Popular metric learners which are based on the classification error of a k nearest neighbor classifier have been proposed in the approaches [56, 20]. A proposal which couples metric learning to the observed regression error has recently been published in the article [2]. Besides computational efficiency, the latter can also be accompanied by formal guarantees. Similar learning theoretical guarantees are available for metric learning within the family of vector quantization techniques [43]. Besides the local metric learning techniques as proposed in this approach [43], quite a few metric learning techniques lend itself towards kernelization, resulting in globally nonlinear data transformations [5].

While advancing the question of how to autonomously determine a good data representation in the context of diverse side information, these approaches have in common that they are restricted to vectorial data, i.e. restricted application scenarios only. First techniques extend these methods to richer data structures, in particular strings, sequences, and trees. A few proposals in this frame are covered in the publications [46, 3, 8, 5]. These techniques often rely on a generative approach and determine metric parameters by a data likelihood optimization. Hence they are restricted to learning from positive examples only, not taking into account prior labels or dissimilar pairs. Exceptions are the proposals [3, 4, 40] which refer to a regression task similar to [2] or a classification task similar to [43], respectively. In the following, we will focus on the latter approach which has been developed within the frame of the priority program ‘Autonomous Learning’ of the DFG. Essentially, it introduces a framework for autonomous metric learning for sequence data in the context of prototype based classification. As an alternative, it would be possible to test the approach [4] for sequence metric adaptation for classification, which is based on a formal notion which quantifies that the neighbors of the given data points are, on average, good as regards the relevant classification, a setting which is particularly suited for a k -nearest neighbor classifier or a representation of sequential data in terms of distances to a set of landmarks. Here, we will focus on a prototype-based representation instead.

3.1 Relational LVQ for sequence data

Learning vector quantization (LVQ) refers to a family of intuitive classification schemes, which have recently attracted increased attention in particular in the context of interpretable models e.g. in biomedical data analysis, on the one side, and life-long learning, on the other side [42, 10, 17, 13, 33, 60]. This is caused by the fact that LVQ inherently relies on a representation of the model in terms of typical prototypes such that an intuitive model inspection as well as a compact data description is delivered by the technique; when referring to a probabilistic formalization of LVQ techniques, this corresponds to data being represented by a mixture of Gaussians – however, unlike classical Gaussian mixture models, the parameters are optimized according to the conditional likelihood of the output label rather than the data itself [44]. Deterministic counterparts such as generalized LVQ (GLVQ) can be designed in such a way that they additionally focus on a good generalization ability in terms of margin maximization.

These approaches have recently been generalized to nonvectorial data structures which are described in terms of pairwise similarities or dissimilarities only, see the article [22] for a general framework. Here, we will exemplarily focus on only one possibility, relational GLVQ (RGLVQ). RGLVQ relies on training data which are characterized by pairwise dissimilarities d_{ij} only, where $i, j \in \{1, \dots, n\}$. These measurements could be the result of an edit distance of sequence data, an alignment for DNA or protein sequences, or pairwise graph distances, for example, depending on the area of application. RGLVQ relies on the assumption of symmetry $d_{ij} = d_{ji}$ and zero diagonal $d_{ii} = 0$. In such cases, there always exists a vectorial embedding of the data such that these distances are induced by a symmetric quadratic form, which is not necessarily positive definite, i.e. a so-called pseudo-euclidean space is present [43]. Within this space, vectorial operations are possible, i.e. we can represent data by vectors \mathbf{x}_i and distances by a quadratic form $d_{ij} = d(\mathbf{x}_i, \mathbf{x}_j)$. Assume data \mathbf{x}_i are labeled $c(\mathbf{x}_i)$. Then, a prototype-based classification model in pseudo-euclidean space is given by representative positions $\mathbf{w}_1, \dots, \mathbf{w}_k$ with labels $c(\mathbf{w}_j)$. It induces the classification

$$\mathbf{x} \mapsto c(\mathbf{w}_j) \text{ where } d(\mathbf{x}, \mathbf{w}_j) \text{ is minimum} \quad (1)$$

of a given point \mathbf{x} (where we refer to its position in the pseudo-euclidean embedding). The aim of a prototype-based classifier is the minimization of the classification error, i.e. the term $\sum_i H(d^+(\mathbf{x}_i) - d^-(\mathbf{x}_i))$ where H refers to the Heaviside function, d^+ to the distance of \mathbf{x}_i from the closest prototype with correct label, and d^- to

the distance from the closest prototype with incorrect label. Since an optimization of the classification error itself is NP hard, GLVQ resorts to an approximation

$$\sum_i \Phi \left(\frac{d^+(\mathbf{x}_i) - d^-(\mathbf{x}_i)}{d^+(\mathbf{x}_i) + d^-(\mathbf{x}_i)} \right) \quad (2)$$

Here, the sigmoidal function Φ is used as approximation for H . In addition, since this form would yield to divergence due to its summands being unlimited, a normalization of the summands by the sum of distances is introduced. It can be shown that this term relates to the hypothesis margin of a classifier, i.e. its minimization accounts for a robust result [43].

This model, however, refers to an explicit pseudo-euclidean embedding of data, which is usually not present. Rather data are characterized by the terms d_{ij} , resulting in the distance matrix D of pairwise distances only. It is always possible to compute an explicit pseudo-euclidean embedding from D , but at cubic costs. RGLVQ offers a way to avoid this explicit embedding, resulting in an equivalent formalization at quadratic costs only. For this purpose, prototype locations are restricted to linear combinations of the form

$$\mathbf{w}_j = \sum_i \alpha_{ji} \mathbf{x}_i \text{ with } \sum_i \alpha_{ji} = 1 \quad (3)$$

Based on this assumption, pairwise distances can be expressed as

$$d(\mathbf{x}_i, \mathbf{w}_j) = [D\alpha_j]_i - \frac{1}{2} \cdot \alpha_j^t D \alpha_j \quad (4)$$

where $\alpha_j = (\alpha_{j1}, \dots, \alpha_{jn})$. This results in the costs

$$\sum_i \Phi \left(\frac{d(\mathbf{x}_i, \mathbf{w}^+) - d(\mathbf{x}_i, \mathbf{w}^-)}{d(\mathbf{x}_i, \mathbf{w}^+) + d(\mathbf{x}_i, \mathbf{w}^-)} \right) \quad (5)$$

with

$$d(\mathbf{x}_i, \mathbf{w}^\pm) = [D\alpha^\pm]_i - \frac{1}{2} \cdot (\alpha^\pm)^t D \alpha^\pm \quad (6)$$

These costs do no longer depend on an explicit vectorial embedding. Hence this formalization allows an optimization of prototype parameters α_j based on D only. Typically, gradient techniques are used in this frame. See the publication [22] for details.

3.2 Autonomous adaptation of sequence metrics within LVQ

While resulting in an efficient classifier for dissimilarity data, the accuracy crucially depends on the quality of the chosen dissimilarity measure and its parameterization. Autonomous metric learning in parallel to prototype adaptation has proved a central ingredient of

state-of-the-art LVQ techniques for vectorial data; in the following, we briefly discuss how this principle can be transferred to discrete symbolic data, i.e. relational LVQ as well. We assume that sequential data are given, i.e. data have the form $\mathbf{Y} = y_1, \dots, y_K$ with length K and entries y_l in some suitable data space Σ , e.g. a real-vector space for sensor signals or a discrete alphabet for bioinformatics sequences.

The alignment distance constitutes one of the most common measures to compare two such sequences with possibly different length: An alignment of two sequences \mathbf{Y} and \mathbf{Z} is an extension of these two sequences by gaps, referenced by $-$, such that the resulting sequences \mathbf{Y}^* and \mathbf{Z}^* have the same length. Having fixed a dissimilarity measure of how to compare sequence entries enriched by the symbol $-$

$$d_\lambda : (\Sigma \cup \{-\}) \times (\Sigma \cup \{-\}) \rightarrow \mathbb{R} \quad (7)$$

which may depend on parameters λ , two aligned sequences \mathbf{Y}^* and \mathbf{Z}^* can easily be compared by summing the distances of all sequence entries y_i^* and z_i^* . The alignment distance $d^*(\mathbf{Y}, \mathbf{Z})$ of two sequences is then defined as the minimum distance of all possible alignments of these sequences.

Usually, the outcome crucially depends on the parameterization λ . Similar to the vectorial case, the optimization of the prototypes in the costs 5 can be accompanied by an adaptation of the parameters λ : the basic idea is to optimize these parameters simultaneously to the model parameters α_{jl} by means of a gradient technique. Hence autonomous metric learning boils down to the question of how to efficiently compute derivatives of the alignment distance with respect to its basic parameters λ . In general, this is not possible since the alignment distance is discontinuous, hence a derivative does not exist. It has been proposed in the recent work [40] to use an efficient approximation of a dynamic programming scheme, instead, as follows: an optimum alignment can easily be computed based on the Bellman optimality principle by dynamic programming, resulting in the central recursion formula

$$\begin{aligned} d^*(\mathbf{Y}(0), \mathbf{Z}(0)) &= 0, \\ d^*(\mathbf{Y}(0), \mathbf{Z}(J)) &= \sum_{j=1}^J d_\lambda(-, z_j), \\ d^*(\mathbf{Y}(I), \mathbf{Z}(0)) &= \sum_{i=1}^I d_\lambda(y_i, -), \end{aligned} \quad (8)$$

$$d^*(\mathbf{Y}(I+1), \mathbf{Z}(J+1)) = \min \left\{ \begin{aligned} &d^*(\mathbf{Y}(I), \mathbf{Z}(J)) + d_\lambda(y_{I+1}, z_{J+1}), \\ &d^*(\mathbf{Y}(I+1), \mathbf{Z}(J)) + d_\lambda(-, z_{J+1}), \\ &d^*(\mathbf{Y}(I), \mathbf{Z}(J+1)) + d_\lambda(y_{I+1}, -) \end{aligned} \right\}.$$

where $\mathbf{Y}(I)$ and $\mathbf{Z}(J)$ refers to the first I or J entries of the sequence \mathbf{Y} or \mathbf{Z} . The latter three choices refer to an optimal alignment by one of the three possibilities, a match of the last sequence entries, an insert or a delete. This recursion formula can be computed in quadratic time. When we substitute the discrete operator \min by the smooth function

$$\text{softmax}(x_1, x_2, x_3) = \sum_i x_i \frac{\exp(-\beta x_i)}{\sum_j \exp(-\beta x_j)} \quad (9)$$

with $\beta > 0$, we arrive at an approximation which allows us to compute the derivative of the alignment distance by means of exactly the same Bellmann principle in quadratic time. This can easily be inserted into a gradient scheme for the costs 5. See [40] for details.

3.3 Experiments

We shortly elucidate the results obtained by autonomous structure metric learning for sequences in two important cases: a discrete symbol alphabet and continuous sequence entries. For this purpose, we consider the following two data sets:

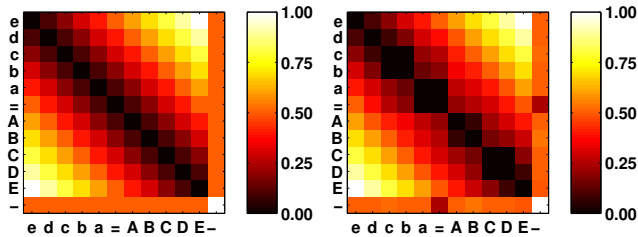


Fig. 1 Left: prior scoring matrix used for sequence comparison; right: posterior scoring matrix optimized according to the given classification task.

Copenhagen Chromosomes:

The data set consists of images of two different chromosomes which are encoded by the differential change of the thickness of the silhouette. The differences are encoded via the discrete alphabet $\Sigma = \{f, \dots, a, =, A, \dots, F\}$, with lower / upper cases encoding negative / positive changes, respectively. Hence every data point corresponds to a sequence with entries in the discrete alphabet Σ .

A comparison of such sequences depends on the local scoring matrix which compares these letters, i.e. a scoring matrix of size $(|\Sigma \cup \{-\}|)^2$ which indicates the costs of substituting one symbol by another (or a gap). This matrix is assumed to be symmetric to account for symmetric dissimilarities D . A reasonable prior assumption is to put a larger weight on large changes within the alphabet, taking into account the differential encoding of the thickness, as shown in Fig.1(left). However, it is not clear whether such prior weighting is optimal for the task.

Online learning of these scores confirms a prior which assigns higher scores to off-diagonals, however a more subtle structure is obtained, see Fig.1(right). The obtained structure is almost independent of the initialization of the scoring matrix. The accuracy obtained when adapting the scoring matrix in addition to the prototypes is presented in Fig.2(top) when initializing scores with the unit matrix and Fig.2(bottom) when initializing with a diagonal weight prior. In both cases, the obtained accuracy approaches 0.95 in a cross-validation. Interestingly, albeit the diagonal weight prior is closer in characteristics to the learned scoring metric than the unit matrix, the latter displays a higher accuracy. This clearly demonstrates the potential of an autonomous metric learning which can take into account subtle differences indicated by the data. See [40] for details as regards the training set and parameters of the algorithm.

Java programs:

The data set consists of java code corresponding to implementations of sorting programs according to the two different strategies Bubblesort and Insertionsort (programs are taken from the internet). Programs are represented as sequences as follows: the Oracle Java Compiler API transforms every program into a syntax tree where every node is described by a number of characteristics (such as return type, type, or scope). These trees are transferred to sequences by prefix notation.

An alignment distance can be rooted in a pairwise comparison of entries which essentially, for every characteristics, tests a match versus mismatch. The challenge is then how to weight the relevance of these single characteristics; a good prior is to use a uniform weighting of every component. In general, a weighted distance measure which assigns the weight λ_l to the similarity of the l th characteristic of a node is taken. Metric learning enables an automated adaptation of these weighting terms λ_l . The result of such relevance learning is depicted in Fig.4 for the sorting data set (see [40] for details of the setup). Interestingly, the relevance weighting

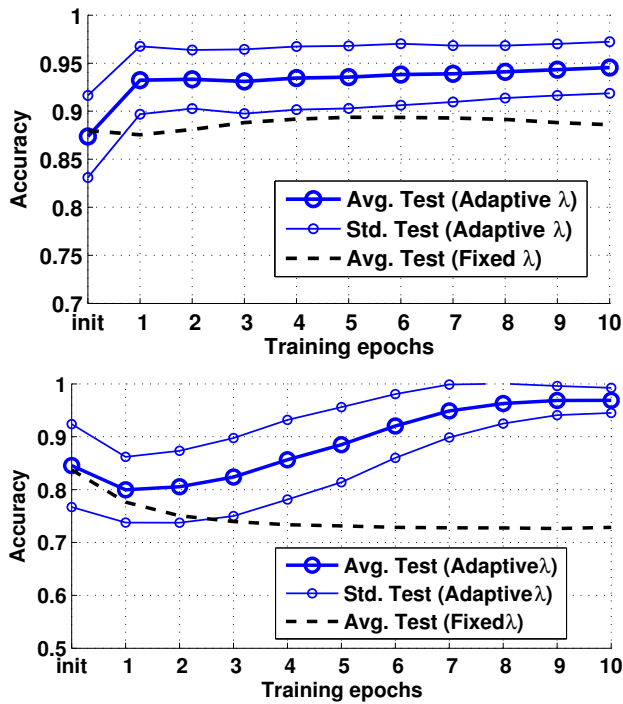


Fig. 2 Accuracy of the chromosome data set with matrix learning when initializing with default values (top) or a band-pattern (bottom).

emphasizes the relevance of a node type as compared to e.g. code position, the latter being not useful for a class discrimination. The classification accuracy can be improved to an average .8 when using the adapted metric (see Fig.3). The metric adaptation corresponds to a different data representation, as can be seen in Fig.5. While classes overlap for the default weighting which assigns the same relevance to every node entry, a task-adapted relevance weighting clearly emphasizes class-separability.

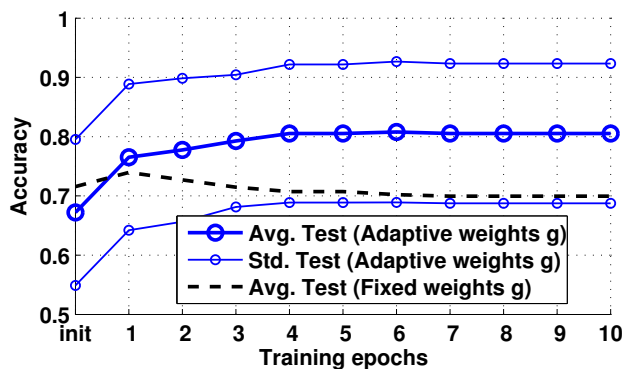


Fig. 3 Accuracy on the sorting data set for an adapted structure metric obtained via cross-validation.

3.4 Software

An efficient realization of differentiable approximations of local and global alignment distances as well as their derivatives and diverse visual inspection technology can be found at <http://openresearch.cit-ec.de/projects/tcs>. These metrics can directly be plugged into relational LVQ, see e.g. http://www.techfak.uni-bielefeld.de/~xzhu/ijcnn14_tutorial.html

3.5 Outlook

We have discussed that the principle of metric learning can be transferred to structured data such as sequences, by means of a seamless integration of relational LVQ and gradient based schemes for the optimization of metric and prototype parameters. While the results are very promising, the approach suffers from a high computational load: the full dissimilarity matrix D has to be computed after every optimization step. In [40], diverse approximation schemes have been proposed, however, it might be worthwhile to also think about an alternative characterization of the distance measure in terms of a linear combination of dissimilarity matrices, for example.

4 Representation learning from sequential data

Conventional automatic speech recognition (ASR) systems rely on supervised learning, where an acoustic model is trained from transcribed speech, and a language model, i.e., the a priori probabilities of the words, from large text corpora. Both, the inventory of word, i.e., the vocabulary, and the inventory of phonemes are fixed and known. Furthermore, a lexicon is given which contains for each word its pronunciation in terms of a phoneme sequence.

Here we consider an unsupervised setting, where neither the pronunciation lexicon nor the vocabulary and the phoneme inventory are known in advance, and

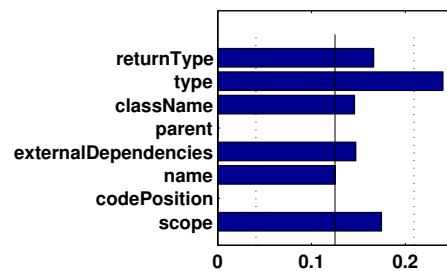


Fig. 4 Relevance weights learned for the weighting of the node entries.

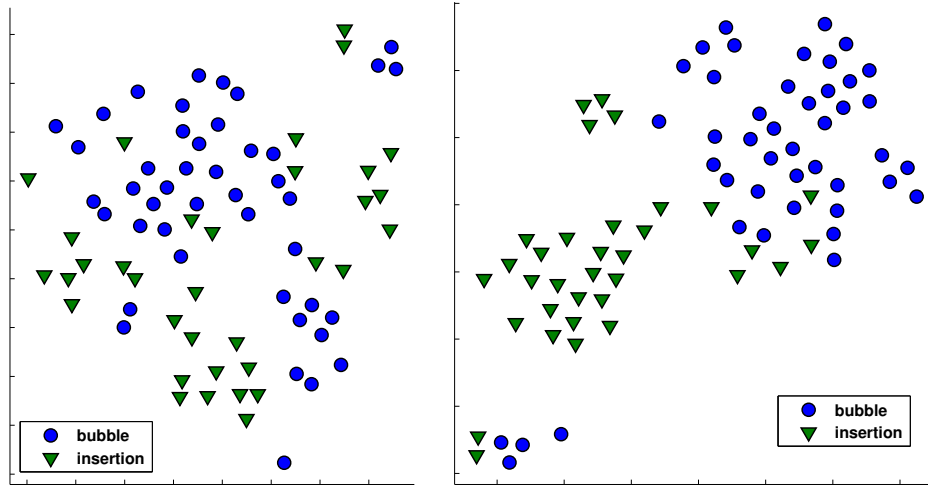


Fig. 5 t-SNE projection of the data based on the standard alignment distance (left) and the adapted metric (right).

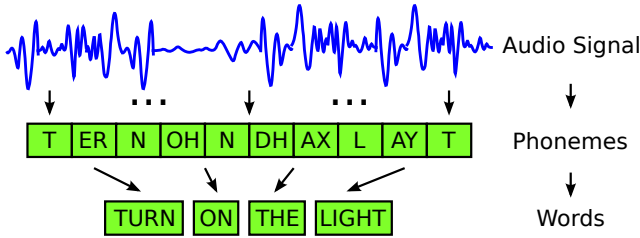


Fig. 6 Hierarchical representation of a speech signal

the acoustic training data come without labels. Referring to the hierarchical nature of speech, we are therefore concerned with the task of unsupervised learning of a deep representation from sensory input, the discovery of the phonetic and lexical inventory.

For speech recognition, an audio recording is typically represented as a time series of real valued vectors of frequency or cepstral coefficients. A symbolic representation is learned by discovering repeated sequences of vectors and assigning the same labels to similar sequences. On this label sequence again similar sequences can be discovered and given labels from another label set, thus arriving at representations at different levels of hierarchy. Figure 6 shows an example of a two level hierarchical representation of a speech signal.

On the first hierarchical level the aim is to discover the acoustic building blocks of speech, the phonemes, and to learn a statistical model for each of them, the acoustic model [11, 55, 53, 47]. In speech recognition, the acoustic model usually consists of Hidden Markov Models (HMMs), where each HMM emits a time series of vectors of cepstral coefficients.

The second level is targeted at the discovery of the lexical units, the words, and learning their probabili-

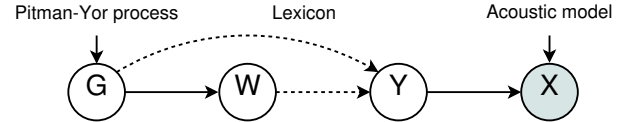


Fig. 7 Graphical model with random variables dependencies for the language Model G , words W , phonemes Y and acoustic feature vectors X . The shaded circle denotes the observations, solid lines probabilistic dependencies and dashed lines deterministic dependencies.

ties, the language model, from the phoneme sequences of the first level [54, 41, 25, 26, 39]. In speech recognition, the mapping of words to phoneme sequences is typically determined by a pronunciation lexicon. So called n -gram language models are used to calculate the probabilities of words, depending on their context, which is given by the $n-1$ preceding words. They usually consist of categorical distributions over words for each context.

Figure 7 shows a graphical model for the dependencies between the random variables. The language Model G and the lexicon are generated from a prior process, the Pitman-Yor process. Then words W are generated using the language model and mapped to phonemes Y using the lexicon. Acoustic feature vectors X are finally generated employing an acoustic model.

In this article we will focus on the autonomous learning of representations on the second level, the discovery of words from phoneme sequences, where the phoneme sequences have been generated by a phoneme recognizer in a supervised fashion, i.e. by the recognition of the speech signal, assuming the phoneme set and acoustic models for each of the phonemes to be known.

Since phoneme recognition from recordings of continuous speech is a difficult task, even if the phoneme inventory is known and their models are trained in ad-

vance, the recognized phoneme sequences will be error-prone. To cater for recognition errors we are going to operate on phoneme lattices. A phoneme lattice is a directed acyclic graph, which contains not only a single recognized phoneme sequence, but also alternatives, in the hope that the correct phoneme sequence is among them. Standard ASR phoneme recognizers are able to output a phoneme lattice together with probabilities for each phoneme in the lattice.

4.1 Word recognition from sequential data

We first consider a supervised scenario, where the pronunciation lexicon and the language model are known. The objective of word recognition, given a phoneme sequence $\mathbf{Y} = y_1, \dots, y_K$ of length K , is to segment the phoneme sequence into the most probable word sequence:

$$\hat{\mathbf{W}} = \arg \max_{\mathbf{W}} P(\mathbf{W}|\mathbf{Y}) = \arg \max_{\mathbf{W}} P(\mathbf{Y}|\mathbf{W})P(\mathbf{W}), \quad (10)$$

where both $\hat{\mathbf{W}} = \hat{w}_1, \dots, \hat{w}_L$, the identity of the words, and the number L of words in the sequence are determined in the course of the maximization. Here $P(\mathbf{Y}|\mathbf{W})$ is given by the lexicon and equals one if the character sequence \mathbf{Y} is a concatenation of the words in \mathbf{W} , and zero else. The probability of a word sequence is calculated employing an n -gram language model, with

$$P(\mathbf{W}) \approx \prod_{l=1}^L P(w_l|w_{l-1}, \dots, w_{l-n+1}) =: \prod_{l=1}^L P(w_l|\mathbf{u}). \quad (11)$$

Here, $P(w_l|\mathbf{u})$ is the probability of the l -th word w_l , given its context $\mathbf{u} = w_{l-1}, \dots, w_{l-n+1}$. It can be estimated on training data. In Bayesian language modeling, additionally a prior probability is incorporated.

4.2 Unsupervised learning from sequential data

We now turn to the case where neither the pronunciation lexicon nor the language model are known, and where we are still left with the task to segment a phoneme string into the most probable word sequence. Here we have to learn the language model together with the words. We use the nested hierarchical Pitman-Yor language model (NHPYLM), denoted by \mathbf{G} , which is a Bayesian language model and allows new, previously unseen words, to evolve and assigns probabilities to them. It is based on the Pitman-Yor process prior, which

produces power-law distributions that resemble the statistics found in natural languages [49, 50, 39].

An n -gram language model $G_{\mathbf{u}}$ is a categorical distribution of probabilities for the N words of the vocabulary: $G_{\mathbf{u}} = \{P(w^1|\mathbf{u}), \dots, P(w^N|\mathbf{u})\}$. In a hierarchical Pitman-Yor process, $G_{\mathbf{u}}$ is modeled as a draw

$$G_{\mathbf{u}} \sim PY(d_{|\mathbf{u}|}, \theta_{|\mathbf{u}|}, G_{\pi(\mathbf{u})}) \quad (12)$$

from a Pitman-Yor process with base measure $G_{\pi(\mathbf{u})}$, strength parameter $d_{|\mathbf{u}|}$ and discount parameter $\theta_{|\mathbf{u}|}$ [50]. The base measure corresponds to the expected probability distribution of the draws and is set to the language model $G_{\pi(\mathbf{u})}$ of the parent $(n-1)$ -gram. This process is repeated until the parent LM is a zerogram. Since in the unsupervised setting the vocabulary size is not known in advance, the zerogram cannot be specified. It is therefore replaced by the likelihood for the word being a phoneme sequence, calculated by a hierarchical Pitman-Yor language model (HPYLM) of phonemes \mathbf{H}' , similar to (11), where again a hierarchy of phoneme language models is built up to some order m , similar to (12). The phoneme zerogram is finally set to a uniform distribution over the phoneme set. The resulting structure is the NHPYLM, which consists of a HPYLM for words and a HPYLM for phonemes.

Since we now have to learn the NHPYLM along with the words, the maximization problem becomes:

$$\begin{aligned} (\hat{\mathbf{W}}, \hat{\mathbf{G}}) &= \arg \max_{\mathbf{W}, \mathbf{G}} P(\mathbf{W}, \mathbf{G}|\mathbf{Y}) \\ &= \arg \max_{\mathbf{W}, \mathbf{G}} P(\mathbf{Y}|\mathbf{W}, \mathbf{G})P(\mathbf{W}|\mathbf{G})P(\mathbf{G}) \\ &= \arg \max_{\mathbf{W}, \mathbf{G}} P(\mathbf{Y}|\mathbf{W})P(\mathbf{W}|\mathbf{G})P(\mathbf{G}) \end{aligned} \quad (13)$$

Here we exploited the fact that \mathbf{Y} is independent of \mathbf{G} if \mathbf{W} is given, since \mathbf{Y} is the concatenation of the phoneme sequences of the words in \mathbf{W} . $P(\mathbf{Y}|\mathbf{W})$ is again either one or zero as before. The difference to equation (10) is, that the nested hierarchical Pitman-Yor process prior $P(\mathbf{G})$ over the language model is introduced. Instead of having one particular language model, we have to find that pair of language model and word sequence which maximizes the joint probability. The maximization is carried out by Gibbs sampling, first sampling the word sequence from $P(\mathbf{W}|\mathbf{Y}, \mathbf{G})$, calculated similar to (10), by keeping \mathbf{G} constant in (13) and then the language model from $P(\mathbf{G}|\mathbf{W})$ [39] in an alternating and iterative fashion.

The previous formulation can be extended to acoustic features \mathbf{X} as input [41]. The maximization problem

Rank	c_w	Phonemes	Characters
1	3489	dh ax	THE
13	447	s eh d	SAID
17	365	m ih s t ax	MISTER
20	327	f ay v	FIVE
23	279	p ax s eh n t	PERCENT
25	268	m ih l ia n	MILLION
26	267	s ah m	SOME
27	263	k ah m p ax n iy	COMPANY
29	259	d oh l ax z	DOLLARS
33	235	hh ae v	HAVE

Table 1 Most often found words with more than 3 characters

In total 28.6% of the words from the running text were correctly discovered (recall) where 32.2% of all the discovered words are correct (precision), resulting in an F-score of 30.3%. The phoneme error rate was reduced to 24.5%. The precision for the lexicon is 13.2% with a recall of 21.8%, resulting in a lexicon F-score of 16.4%. Out of the 100 most often found words, 80 were correct words. Our implementation needed a runtime of about 10 hours for the 100 iterations on a single core of an Intel(R) Xeon(R) E5-2640 at 2.50GHz resulting in a realtime factor of one.

An overview and evaluation of algorithms for acoustic model and word discovery can be found in [31]. These algorithms, however, don't consider recognition errors in the phoneme sequences as we do. Word discovery on noisy phoneme lattices was also considered in [41], using similar methods. A comparison in [26] showed greatly improved F-scores of our proposed method compared to [41] for word n -grams greater than 1. This is due to a more consistent use of the language model hierarchy combined with our iterative approach, making it computationally feasible. For a more detailed analysis see [25].

4.4 Software

We implemented the algorithm using weighted finite state transducers (WFSTs) and the OpenFst library. The implementation is available as a download at <http://nt.uni-paderborn.de/mitarbeiter/oliver-walter/software/>.

4.5 Outlook

Due to the high variability of speech within and especially across speakers, a single word can have different phoneme transcriptions. Recognition errors will also lead to different phoneme sequences. Two examples can be found in the 100 most often found words. The number 100 was discovered as “hh ah n d ax d” and “hh ah

n d r ih d” and the number 90 as “n ay n t iy” and “n ey t iy”. A combination with metric learning and clustering of similar words with different pronunciations or spelling errors, could improve the learning result.

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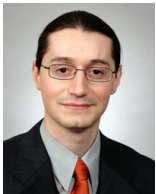
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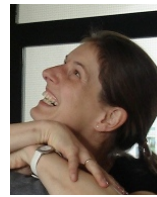


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