A tree-form constant market share analysis
for modelling growth causes in international trade*

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Abstract

This paper introduces a tree-form constant market share (CMS) analysis for modelling growth causes in international trade between a focus country and a single destination based on a complex data set classified at three levels. Basic properties of this model are investigated briefly. The application of this model is discussed in detail. The tree-form CMS is a collection of the CMS models at different levels, including the entire, branch- and leaf-models, which consists of a large amount of information and has a wide application spectrum. It is found that if the market shares for all commodities are both homogenous in the initial and final years, respectively, or if the market growth in all of the categories is the same, the three level-effects will all vanish. Then the tree-form CMS model is applied to analyze the growth causes of China’s exports to Germany, particularly in agricultural products. Our results indicate that the growth causes before China’s accession to WTO (or the 2008 financial crisis) and thereafter are clearly different. Our theoretical findings are also confirmed by those data examples. Finally, some of the outputs of the tree-form CMS model are further analyzed using suitable statistical approaches.

Keywords: Tree-form CMS; growth causes; international trade; structural breaks

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1. Introduction

Constant market share (CMS) analysis, also known as shift-share analysis, is an accounting method for decomposing a country’s export change into the “demand growth”, “competitive” and “interaction” effects, which was first applied to empirical studies in industrial and regional economics. CMS analysis became popular in empirical international economics with the pioneering work of Tyszynski (1951) and it has been increasingly used and refined despite continued criticism both on its theoretical and empirical aspects (Richardson, 1971, Jepma, 1986 and Milana, 1988). In recent years, in addition to its application in international economics (Chen et al., 2000 and Guo et al., 2010), CMS analysis is also widely applied in other fields, such as tourisms, energy economics and firm performance. Moreover, results of the CMS model can be used for further statistical analysis (Batista, 2008) to obtain detailed information for decision making. The purpose of this paper is to introduce a tree-form CMS for modelling trade between a focus country (A) and a destination (B) based on data classified at several levels, to investigate the basic properties of this proposal and to discuss its application. We will see that the tree-form CMS extends the application spectrum of the CMS analysis clearly. For further discussion on the detailed theoretical properties of the tree-form CMS model, the comparison between this model and other well known CMS models and its possible extensions we refer the reader to Feng et al. (2011).

At first, the change of A’s exports to B can be decomposed at different levels of classified data and an entire three-level tree-form CMS model is defined based on the third-level decomposition. Analogously, the i-th first-level, the (i, j)-th second-level branch-model and the (i, j, k)-th leaf-model are defined by taking the corresponding element out of the entire three-level tree-form CMS model, respectively. It is found that the level-effects caused by the classification have some interesting properties. In particular, it is shown that, under certain special conditions, all or some of the level-effects will be zero, positive or negative. Then China’s exports to Germany are taken as an example to show our findings and to analyze the growth causes. From the results of decomposition, we also see that remarkable economic events, e.g. China’s accession to WTO and the 2008 financial crisis, exhibited clearly different impacts on the growth causes. Last but not least, the outputs of the branch-model for industrial products are chosen to show the developments of the demand growth, competitive and interaction components. Significant structural breaks in those quantities between 1994 and 2008 are detected by adapting the approach proposed by Guo et al. (2010). It shows that the outputs of the CMS model can be used as inputs of other statistical models for further analysis.

The paper is organized as follows. The tree-form CMS model is defined in Section 2. Its basic properties are investigated in Section 3. Application of the proposal to China’s exports to Germany is reported in Section 4. Section 5 provides some examples for further statistical analysis of the CMS outputs. The paper is finished by concluding remarks in Section 6.
2. The tree-form CMS model

For simplicity, data classified at three levels will only be considered. That is A’s aggregate exports are first divided into \( n \) first-level categories, the \( i \)-th first-level category consists of \( n_i \) second-level sub-categories and the \((i, j)\)-th second-level category is again composed of \( n_{ij} \) third-level sub-categories. B’s total imports from the world are classified in the same way. Denote the quantities of A’s exports at those classification levels in the initial and final years by \( q_i^0, q_i^1; q_{ij}^0, q_{ij}^1 \) and \( q_{ijk}^0, q_{ijk}^1 \), \( i = 1, \ldots, n, j = 1, \ldots, n_i, \) and \( k = 1, \ldots, n_{ij} \), the quantities of B’s imports from the world by \( Q_i^0, Q_i^1; Q_{ij}^0, Q_{ij}^1 \) and \( Q_{ijk}^0, Q_{ijk}^1 \) and A’s corresponding market shares by \( s_i^0, s_i^1; s_{ij}^0, s_{ij}^1 \) and \( s_{ijk}^0, s_{ijk}^1 \), respectively. We have \( q_i^0 = \sum_{j,k} q_{ijk}^0 = \sum_{i,j,k} q_{ijk}^0 \), where \( \sum \) and \( \sum \) denote double and triple sums over \( i \) and \( j \), and over \( i, j \) and \( k \).

Let \( \Delta \) denote the change between the initial and final years. The change of A’s aggregate exports can be decomposed based on data at different levels of classification:

\[
\Delta q = s^0 \Delta Q + \Delta s Q^0 + \Delta s \Delta Q \quad \text{(overall decomposition)}
\]

\[
= \sum_i s_i^0 \Delta Q_i + \sum_j \Delta s_j Q^0_j + \sum_k \Delta s_k \Delta Q_k \quad \text{(first – level decomposition)}
\]

\[
= \sum_{i,j} s_{ij}^0 \Delta Q_{ij} + \sum_{i,j} \Delta s_{ij} Q^0_{ij} + \sum_k \Delta s_k \Delta Q_{ij} \quad \text{(second – level decomposition)}
\]

\[
= \sum_{i,j,k} s_{ijk}^0 \Delta Q_{ijk} + \sum_{i,j,k} \Delta s_{ijk} Q^0_{ijk} + \sum_k \Delta s_k \Delta Q_{ijk} \quad \text{(third – level decomposition)}
\]

where the three terms in each row on the right-hand-side (rhs) are called the “demand growth component \((D_1)\)”, “competitive component \((C_1)\)” and “interaction component \((I_1)\)”, \( l = 0, 1, 2, 3 \), respectively, calculated at the overall to the third-level using the aggregated, the first-, second- and third-level classified data. These three terms at each level can be called basic decompositions of the total change. In this paper we propose to decompose each of the three CMS components further in a symmetrical way. Based on the third-level decomposition in the fourth row of Model (1), the entire (three-level) tree-form CMS model is defined by

\[
\Delta q = s^0 \Delta Q + \Delta s Q^0 + \Delta s \Delta Q
\]

\[
+ \left[ \sum_i s_i^0 \Delta Q_i - s^0 \Delta Q \right] + \left[ \sum_j \Delta s_j Q^0_j - \Delta s Q^0 \right] + \left[ \sum_k \Delta s_k \Delta Q_k - \Delta s \Delta Q \right]
\]

\[
+ \left[ \sum_{i,j} s_{ij}^0 \Delta Q_{ij} - \sum_i s_i^0 \Delta Q_i \right] + \left[ \sum_{i,j} \Delta s_{ij} Q^0_{ij} - \sum_j \Delta s_j Q^0_j \right] + \left[ \sum_k \Delta s_k \Delta Q_{ij} - \sum_{i,j} \Delta s_{ij} \Delta Q_k \right]
\]

\[
+ \left[ \sum_{i,j,k} s_{ijk}^0 \Delta Q_{ijk} - \sum_{i,j} s_{ij}^0 \Delta Q_{ij} \right] + \left[ \sum_{i,j,k} \Delta s_{ijk} Q^0_{ijk} - \sum_{i,j} \Delta s_{ij} Q^0_{ij} \right] + \left[ \sum_k \Delta s_k \Delta Q_{ijk} - \sum_{i,j} \Delta s_{ijk} \Delta Q_k \right]
\]
where the three terms in the first row on the rhs of Model (2) are the overall components \((D_0, C_0\text{ and } I_0)\), and those in the second, third and fourth rows are the first-, second- and third-level effects, which are called the demand growth effect \((E^D_i)\), competitive effect \((E^C_i)\) and interaction effect \((E^I_i)\) \((i = 1, 2, 3)\), respectively. Note that in this paper, the concept “component” stands for a main term according to the CMS decomposition and the concept “effect” for the difference between same-named components at two levels over each other. Also note that the sum of the level-effects at each level or within any (sub-) category is always zero, which will be confirmed by data examples in Section 3. Due to the data structure under consideration, the order of the indices \(i, j\) and \(k\) for each sum is fixed and the indices are not exchangeable. This fact rolls out a possible problem in a CMS formulation caused by the order of decomposition, because this is determined in the current context by the nature of the data. Model (2) includes all level-effects due to the classification and provides us detailed sources that cause the change of exports.

Furthermore, the \(i\)-th first-level branch-model is defined by taking the \(i\)-th element out of Model (2), which can be written as follows:

\[
\Delta q_i = s^0_i \Delta Q_i + \Delta s_i Q^0_i + \Delta s_i \Delta Q_i + \left( \sum_j s^0_i \Delta Q_{ij} - s^0_i \Delta Q_i \right) + \left( \sum_j \Delta s_j Q^0_{ij} - \Delta s_i Q^0_i \right) + \left( \sum_j \Delta s_j \Delta Q_{ij} - \Delta s_i \Delta Q_i \right) + \sum_{j,k} \left( s^0_{ij} \Delta Q_{ijk} - s^0_{ij} \Delta Q_{ij} \right) + \left( \sum_k \Delta s_{ijk} Q^0_{ijk} - \Delta s_{ij} Q^0_{ij} \right) + \left( \sum_k \Delta s_{ijk} \Delta Q_{ijk} - \Delta s_{ij} \Delta Q_{ij} \right),
\]

where the terms in the first row on the rhs are the first-level components \((D_1, C_1\text{ and } I_1)\), and those in the second and third rows are the second- and third-level effects, denoted by \(E^D_1, E^C_1, E^I_1\) and \(E^D_2, E^C_2, E^I_2\), \(E^D_3, E^C_3, E^I_3\), respectively. We can define the \((i, j)\)-th second-level branch-model by taking the \((i, j)\)-th element out of Model (2):

\[
\Delta q_{ij} = s^0_{ij} \Delta Q_{ij} + \Delta s_{ij} Q^0_{ij} + \Delta s_{ij} \Delta Q_{ij} + \left( \sum_k s^0_{ijk} \Delta Q_{ijk} - s^0_{ij} \Delta Q_{ij} \right) + \left( \sum_k \Delta s_{ijk} Q^0_{ijk} - \Delta s_{ij} Q^0_{ij} \right) + \left( \sum_k \Delta s_{ijk} \Delta Q_{ijk} - \Delta s_{ij} \Delta Q_{ij} \right),
\]

where the three terms in the first row on the rhs are the second-level components \((D_{2ij}, C_{2ij}\text{ and } I_{2ij})\), and those in the second row are the third-level effects, denoted by \(E^D_{3ij}, E^C_{3ij}\) and \(E^I_{3ij}\), respectively. Finally, the \((i, j, k)\)-th leaf-model can be defined for each final (leaf-) category by taking the \((i, j, k)\)-th element out of Model (2):

\[
\Delta q_{ijk} = s^0_{ijk} \Delta Q_{ijk} + \Delta s_{ijk} Q^0_{ijk} + \Delta s_{ijk} \Delta Q_{ijk},
\]

where the terms on the rhs are the third-level components \((D_{3ijk}, C_{3ijk}\text{ and } I_{3ijk})\). Note that all of the
branch- and leaf-models are parts of Model (2). Particularly, each branch-model looks like another tree-form CMS model defined based on data from that level to the final categories. In summary, Models (2) to (5) constitute a collection of the CMS models at different levels, which consists of a large amount of information and has a wide application spectrum. For further extensions of the tree-form CMS model see Feng et al. (2011).

3. Properties of the tree-form CMS model

Now we will discuss the sources of the level-effects. The following theorem provides conditions under which some or all of the level-effects $E_i^0, E_i^C$ and $E_i^l$ vanish. Proofs of the results may be found in Feng et al. (2011).

**Theorem 1**: Under the regularity conditions $q_i^0, q_i^l, Q_i^0$ and $Q_i^l > 0$, we have

Case 1: a) If $s_1^0 = s_2^0 = \ldots = s_n^0$, then $E_i^0$ vanishes;

b) If $s_1^l = s_2^l = \ldots = s_n^l$, then $E_i^C$ vanishes and

c) If both conditions in a) and b) are fulfilled, then $E_i^0, E_i^C$ and $E_i^l$ all vanish.

Case 2: If $Q_i^l : Q_i^0 = Q_2^l : Q_2^0 = \ldots = Q_n^l : Q_n^0$, then all of the three first-level effects vanish.

Theorem 1 reveals a more deep relationship between different variables so that the level-effects vanish, which can also be extended to effects at other levels. All conditions in Cases 1 and 2 are sufficient, but may be unnecessary. In the following we will call $q_i^0$ and $q_i^l$ endogenous and $Q_i^0$ and $Q_i^l$ exogenous quantities, which reflect A's export structure and its changes, and B's market structure and its changes, respectively. Conditions in Case 1 show if the market shares are the same for all commodities in the initial and final years, respectively, all of the three level-effects caused by the classification will vanish. These conditions can be regarded as suitable mixed conditions, because the market shares depend on $q_i^0$ and $q_i^l$, and $Q_i^0$ and $Q_i^l$, simultaneously, which indicate the inhomogeneity of A's market share in different commodities is one of the sources of the level-effects. The homogeneity assumption on A's market share is irrelevant in practice. Conditions in Case 2 are suitable exogenous conditions, which only depend on B's market situation and demonstrate that, if the market growth in each of the $n$ categories is the same, all of the three level-effects will be zero. Now the change of exports is mainly reflected by the overall components. The inhomogeneity of the market growth in different commodities is another source of the level-effects.

Data examples in Section 3 show the market growth is sometimes roughly homogeneous.

The special case with $n = 2$ is taken to show some details. Note that now the sufficient condition in Case 2 of Theorem 1 becomes $Q_1^l Q_1^0 = Q_2^l Q_2^0$. Let iff stand for *if and only if*. 

5
Corollary 1: Assume that the regularity conditions of Theorem 1 hold. For \( n = 2 \) we have

a) \( E^0_i > 0 (= 0 \text{ or } < 0) \), iff \( (Q^0_i Q^1_i - Q^0_i Q^0_i)(s^0_i - s^0_j) < 0 (= 0 \text{ or } > 0) \);

b) \( E^C_i > 0 (= 0 \text{ or } < 0) \), iff \( (Q^0_i Q^1_i - Q^0_i Q^0_i)(s^1_j - s^0_j) > 0 (= 0 \text{ or } < 0) \);

c) \( E^1_i > 0 (= 0 \text{ or } < 0) \), iff \( (Q^0_i Q^1_i - Q^0_i Q^0_i)(s^0_i - s^0_j)Q^1_i - (s^1_j - s^0_j)Q^0_i > 0 (= 0 \text{ or } < 0) \) and

d) The effects \( E^0_i, E^C_i \) and \( E^1_i \) all vanish, iff \( Q^0_i Q^1_i = Q^0_i Q^0_i \) or \( s^0_i = s^0_j \) and \( s^1_j = s^0_j \).

Corollary 1d) shows that, for \( n = 2 \), conditions of Theorem 1 such that the three terms all vanish are also necessary. Corollaries 1 a) to c) indicate further when the level-effects \( E^0_i, E^C_i \) and \( E^1_i \) will be positive, zero or negative. Once one of the three terms vanishes, the other two are equal in absolute value and opposite in sign. Furthermore, if \( (s^0_i - s^0_j)Q^1_j - (s^1_j - s^0_j)Q^0_i = 0 \) but \( Q^0_i Q^1_j - Q^0_i Q^0_i \neq 0 \), \( s^0_i \neq s^0_j \) and \( s^1_j \neq s^0_j \), then the first-level interaction effect \( E^1_i \) is fully divided into \( E^0_i \) and \( E^C_i \) with weights determined by \( Q^0_i \) and \( Q^1_i \). For \( n > 2 \), necessary conditions such that \( E^0_i, E^C_i \) and \( E^1_i \) all vanish become more complex and will not be discussed.

4. Decomposing growth causes of China’s exports to Germany

Data downloaded from the United Nations Commodity Trade Statistics Database (UN Comtrade) are used as examples. In this section, results for the periods from 2000 to 2001, 2001 to 2002, 2007 to 2008 and 2008 to 2009 will be discussed in detail. Those periods are chosen around China’s accession to WTO and the 2008 financial crisis, which have strongly affected the trade relationship between China and Germany (Guo et al., 2010). According to the Standard International Trade Classification (SITC Rev. 3, shortly SITC), total exports are divided into two first-level categories, i.e. agricultural and industrial products. Based on the 1-digit SITC, agricultural products are composed of four categories (SITC 0, 1, 2 and 4), and industrial products consist of four categories (SITC 5-8), which are the eight second-level categories considered. SITC 3 and 9 are excluded due to many missing values. Then based on the 2-digit SITC, the four agricultural categories are composed of ten, two, nine and three, and the four industrial categories are divided into nine, nine, nine and eight sub-categories, respectively. These are regarded as the third-level categories.

At first, the results of the three-level tree-form CMS model, Model (2), are listed in Table 1, which show that each sum of the effects at the first-, second- and third-level is zero. For instance, in China’s exports to Germany from 2008 to 2009, the three third-level effects are 1214, -1612 and 398 million US dollars, respectively, which sum up to zero. Results of Corollary 1 can be now confirmed numerically. Firstly, the three first-level effects of China’s exports to Germany from 2000 to 2001 are all about zero. According to Corollary 1 c), this can only happen if \( Q^1_i : Q^0_i = Q^2_i : Q^0_i \) or \( s^0_i = s^0_j \) and \( s^1_i = s^1_j \). After detailed checking, we find \( s^0_i \neq s^0_j \) and \( s^1_i \neq s^1_j \), but \( Q^1_i : Q^0_i = \ldots \).
50.9:48.2≈1.06:1 and \( Q_2^1:Q_2^0 = 370.6:348.7 \approx 1.06:1 \) and conditions of Corollary 1 d) are roughly fulfilled. By China’s exports to Germany from 2007 to 2008 the first-level demand growth effect \( (E^0_1) \) is negative and the first-level competitive effect \( (E^c_1) \) is positive. The reasons for this are \( (Q^0_1-Q^0_0)(s^1_1-s^0_2) > 0 \) and \( (Q^0_1-Q^0_0)(s^1_1-s^0_2) > 0 \), according to Corollaries 1 a) and b). Results in Table 1 also show that the absolute values of the second- or third-level effects may also be larger than that of the corresponding first-level effect.

Table 1: Results of the entire three-level tree-form CMS model ($US million)

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Effect</td>
<td>( D )</td>
<td>( C )</td>
<td>( I )</td>
<td>( D )</td>
</tr>
<tr>
<td>Overall</td>
<td>573</td>
<td>-95.0</td>
<td>-5.9</td>
<td>195</td>
</tr>
<tr>
<td>( E_1 )</td>
<td>4.3</td>
<td>-3.9</td>
<td>-0.46</td>
<td>-22.7</td>
</tr>
<tr>
<td>( E_2 )</td>
<td>-61.1</td>
<td>57.4</td>
<td>3.7</td>
<td>-19.1</td>
</tr>
<tr>
<td>( E_3 )</td>
<td>85.3</td>
<td>-77.2</td>
<td>-8.1</td>
<td>-71.2</td>
</tr>
</tbody>
</table>

Because the total exports consist of two first-level categories, i.e. agricultural and industrial products, we have two first-level branch-models. We will focus on agricultural products. Corresponding results following Model (3) are given in Table 2. Table 2 confirms again that \( E^0_{21} + E^c_{21} + E^l_{21} = 0 \) and \( E^0_{31} + E^c_{31} + E^l_{31} = 0 \) hold. It is found that all of the three second-level effects of China’s exports to Germany in agricultural products from 2001 to 2002 are relatively very small, because Germany’s market growth in the four sub-categories of agricultural products during that period was roughly homogeneous with \( Q^0_1:Q^0_2:Q^0_3 \approx 1:0.17:0.52:0.04 \) and \( Q^l_1:Q^l_2:Q^l_3 \approx 1:0.17:0.52:0.04 \). That is, the condition of Case 2 in Theorem 1 is approximately fulfilled.

Table 2: Results of the first-level branch-model for agricultural products ($US million)

<table>
<thead>
<tr>
<th>Effect</th>
<th>( D_{11} )</th>
<th>( C_{11} )</th>
<th>( I_{11} )</th>
<th>( E^0_{21} )</th>
<th>( E^c_{21} )</th>
<th>( E^l_{21} )</th>
<th>( E^0_{31} )</th>
<th>( E^c_{31} )</th>
<th>( E^l_{31} )</th>
</tr>
</thead>
<tbody>
<tr>
<td>00-01</td>
<td>26.2</td>
<td>21.0</td>
<td>1.2</td>
<td>-0.17</td>
<td>-3.0</td>
<td>3.2</td>
<td>12.9</td>
<td>-11.9</td>
<td>-0.97</td>
</tr>
<tr>
<td>01-02</td>
<td>25.9</td>
<td>-27.4</td>
<td>-1.4</td>
<td><strong>-1.2</strong></td>
<td><strong>1.2</strong></td>
<td><strong>0.04</strong></td>
<td>-4.5</td>
<td>4.7</td>
<td>-0.2</td>
</tr>
<tr>
<td>07-08</td>
<td>201</td>
<td>72.3</td>
<td>10.0</td>
<td>9.3</td>
<td>-6.7</td>
<td>-2.7</td>
<td>-33.5</td>
<td>33.1</td>
<td>0.45</td>
</tr>
<tr>
<td>08-09</td>
<td>-303</td>
<td>174</td>
<td>-30.3</td>
<td>26.4</td>
<td>-14.6</td>
<td>-11.7</td>
<td>135</td>
<td>-176</td>
<td>40.6</td>
</tr>
</tbody>
</table>

Both agricultural and industrial products are composed of four second-level categories, so there are totally eight second-level branch-models. According to the 1-digit SITC, we have chosen food and live animals (0), and machinery and transport equipment (7) as examples. Results of these two
chosen second-level branch-models are shown in Table 3. It is clear that after China’s accession to WTO, the competitive component had a great drop from 36.2 to -20.4 million US dollars for food and live animals, which however exhibited a huge increment from 298 to 1145 million US dollars for machinery and transport equipment. This fact indicates that for export competitiveness, China’s accession to WTO had a negative short-term impact on agricultural products but a positive impact on industrial products.

Table 3: Results of the chosen second-level branch-models ($US million)

<table>
<thead>
<tr>
<th>Effect</th>
<th>Food and live animals</th>
<th>Machinery and transport equipment</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$D_{211}$</td>
<td>$C_{211}$</td>
</tr>
<tr>
<td>00-01</td>
<td>30.4</td>
<td>36.2</td>
</tr>
<tr>
<td>01-02</td>
<td>22.5</td>
<td>-20.4</td>
</tr>
<tr>
<td>07-08</td>
<td>161</td>
<td>0.84</td>
</tr>
<tr>
<td>08-09</td>
<td>-97.0</td>
<td>33.6</td>
</tr>
</tbody>
</table>

Finally, two 2-digit SITC commodities, i.e. fish, etc. (03) and office machines, etc. (75) are chosen to show the results of the leaf-models. Results for these two models are provided in Table 4. The total export change of fish and office machines are -6.32 and -2920 million US dollars from 2008 to 2009, respectively, caused by the financial crisis. The large reduction is mostly caused by the demand growth component, because the import demand in Germany decreased significantly. The 2008 financial crisis had a clearly negative short-term impact on China’s exports of agricultural and industrial products. We see, each leaf-model based on each third-level category can still provide us very detailed information that causes the change of exports.

Table 4: Results of the chosen leaf-models ($US million)

<table>
<thead>
<tr>
<th>Effect</th>
<th>Fish, crustaceans, mollusks, etc.</th>
<th>Office and automatic data-processing</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$D_{3113}$</td>
<td>$C_{3113}$</td>
</tr>
<tr>
<td>00-01</td>
<td>15.9</td>
<td>10.1</td>
</tr>
<tr>
<td>01-02</td>
<td>-2.5</td>
<td>-8.3</td>
</tr>
<tr>
<td>07-08</td>
<td>23.9</td>
<td>84.1</td>
</tr>
<tr>
<td>08-09</td>
<td>-3.6</td>
<td>-2.7</td>
</tr>
</tbody>
</table>

5. Further analysis of the CMS outputs

Now we will use the decompositions for industrial products to show that it is worthy to analyze the CMS results further. The demand growth, competitive and interaction components in this class from
1994 to 2009 are displayed in Figure 1. We see both the demand growth and interaction components exhibited a great drop, i.e., a structural break, in 2009 due to the financial crisis, which however did not happen in the competitive component. Furthermore, there is a clear positive jump in the interaction component between 2002 and 2003, which may indicate the impact of China’s accession to WTO on the growth causes of its exports to Germany. To investigate this in detail, a simple linear or a constant regression model with a rolling dummy variable either in the intercept or in the slope is applied to all series (without the value in 2009). See also Guo et al. (2010) for a related proposal. Then the AIC is used to detect a possible structural break. It is found that all of the three series exhibit a highly significant positive structural break between 2002 and 2003 with $\hat{t} = 10$. The finally selected models are: $\hat{y}_t = 220.64 + 268.69 D_t^R$ with $r^2 = 0.882$ and $p = 2.13 \times 10^{-3}$ for the demand growth component, $\hat{y}_t = 559.34 + 251.18 D_t^R$ with $r^2 = 0.7863$ and $p = 1.06 \times 10^{-5}$ for the competitive component and $\hat{y}_t = -2.494 + 481.279 D_t^L$ with $r^2 = 0.9293$ and $p = 7.438 \times 10^{-9}$ for the interaction component, where $t = 1, \ldots, 15$, $D_t^L = D_t^R = 0$ for $t < 10$, $D_t^L = 1$ and $D_t^R = t$ for $t \geq 10$. We see the structural break in the demand growth and competitive components is a rate-shift, while the interaction component exhibits a level-shift. Note that the last model is equivalent to the result selected by maximizing the $F$-value, if an ANOVA is applied to all pairs of sub-series divided by a rolling time point.

![Figure 1](image_url)

**Figure 1:** Developments of the demand growth, competitive and interaction components ($US million$).

We can also see that the development of the demand growth component between 1994 and 2008 is relatively regular, the variation in the interaction component between 2003 and 2008 is clearly larger than before and that in the competitive component is very large. Moreover, competitive components seem to correlate to each other in a negative way. This means that if China’s competitiveness increased strongly in one year, its increment in the next year tends to be smaller. Results of the Durbin-Watson test and the correlogram show that this negative correlation is however insignificant at the 5%-level.
6. Final remarks

This paper introduces a tree-form CMS model and provides a deep discussion on its application. It is clear that the tree-form CMS model can be easily extended to multi-level classified data (Feng et al., 2011). It is also indicated that, when using the CMS model, not only the final but also the intermediate results contain useful information for decision making. Sources of effects caused by each level of classification are discussed in detail. It is found that if the market shares for all commodities are both homogenous in the initial and final years, respectively, or if the market growth in all of the categories is the same, the three level-effects will all vanish. The tree-form CMS model is applied to analyze the growth causes of China’s exports to Germany, particularly in agricultural products. These data examples also confirmed our theoretical findings. Furthermore, it is found that the growth causes before and after China’s accession to WTO (or the 2008 financial crisis) are clearly different. Finally, analysis of the outputs of the branch-model for industrial products shows that China’s accession to WTO has had a positive long-term impact on all of the three CMS components. In summary, despite a huge number of theoretical studies on the CMS model and its wide applicability, there still seems to be a big play room for the further development of theory and practice of the constant market share analysis. The current paper may open a new research direction in this area.

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References


